



## Werkzeuge zur Behandlung von linearen Gleichungssystemen

|            | Bibliotheken   | Abgeschlossene Programme             |
|------------|--|--------------------------------------|
| symbolisch | muParser (C++, C#)   | Maple<br>Mathematica<br>MuPad<br>... |
| numerisch  | IMSL<br>NAG<br>LAPACK / BLAS<br>LINPACK<br>Numerical Recipes<br>matplotlib (Python)<br>... | Matlab<br>Scilab<br>Octave<br>...    |

### Matlab

Mit Hilfe von Matlab können viele Analysemethoden einfach angewandt werden. Matlab basiert auf effizienten Berechnungsmethoden der linearen Algebra.

```
A = [ 1 2 4; 2 13 23; 4 23 77 ]
b = [ 3 -4 5 ]'
A * b
A \ b
inv(A)
inv(A) * b
L = chol(A)'
[ L, U ] = lu(A)
L * U
[ Q, R ] = qr(A)
Q * R
pinv([ 1 2 4 7; 2 13 23 30; 4 23 77 100 ])
pinv([ 1 2 4; 2 13 23; 4 23 77; 8 33 140 ])
```

### Maple

Maple ermöglicht das symbolische Rechnen mit dem Computer.

```
with(linalg);
A := matrix(3, 3, [ [ 1, 2, 4 ], [ 2, 13, 23 ], [ 4, 23, 77 ] ]);
b := vector(3, [ 3, -4, 5 ]);
inverse(A);
multiply(inverse(A), b);
linsolve(A, b);
A := matrix(3, 3, [ [ a11, a21, a31 ], [ a12, a22, a32 ],
                     [ a13, a23, a33 ] ]);
b := vector(3, [ b1, b2, b3 ]);
inverse(A);
multiply(inverse(A), b);
linsolve(A, b);
```



## LAPACK/BLAS:

Die numerische Bibliothek LAPACK stellt eine umfassende Sammlung hochentwickelter Numerik-Unterprogramme für die Analyse linearer Probleme dar. Sie greift für die Elementarrechnungen auf die maschinenabhängig optimierte Bibliothek BLAS zurück.

### NAME

```
DGETRF - compute an LU factorization of a general M-by-N
matrix A using partial pivoting with row interchanges
```

### SYNOPSIS

```
SUBROUTINE DGETRF( M, N, A, LDA, IPIV, INFO )
INTEGER           INFO, LDA, M, N
INTEGER           IPIV( * )
DOUBLE PRECISION A( LDA, * )
```

### PURPOSE

DGETRF computes an LU factorization of a general M-by-N matrix A using partial pivoting with row interchanges.  
The factorization has the form

$$A = P * L * U$$

where P is a permutation matrix, L is lower triangular with unit diagonal elements (lower trapezoidal if m > n), and U is upper triangular (upper trapezoidal if m < n).

This is the right-looking Level 3 BLAS version of the algorithm.

### ARGUMENTS

|      |   |
|------|---|
| M    | (input) INTEGER   |
|      | The number of rows of the matrix A. M >= 0.   |
| N    | (input) INTEGER   |
|      | The number of columns of the matrix A. N >= 0.  |
| A    | (input/output) DOUBLE PRECISION array, dimension (LDA,N)  |
|      | On entry, the M-by-N matrix to be factored. On exit, the factors L and U from the factorization   |
|      | $A = P * L * U$ ; the unit diagonal elements of L are not stored.   |
| LDA  | (input) INTEGER   |
|      | The leading dimension of the array A. LDA >= max(1,M).  |
| IPIV | (output) INTEGER array, dimension (min(M,N))  |
|      | The pivot indices; for $1 \leq i \leq \min(M,N)$ , row i of the matrix was interchanged with row IPIV(i).   |
| INFO | (output) INTEGER  |
|      | = 0: successful exit  |
|      | < 0: if INFO = -i, the i-th argument had an illegal value   |
|      | > 0: if INFO = i, $U(i,i)$ is exactly zero. The factorization has been completed, but the factor U is exactly singular, and division by zero will occur if it is used to solve a system of equations. |

### NAME

```
DGETRS - solve a system of linear equations A * X = B or
A' * X = B with a general N-by-N matrix A using the LU
factorization computed by DGETRF
```

### SYNOPSIS

```
SUBROUTINE DGETRS( TRANS, N, NRHS, A, LDA, IPIV, B, LDB, INFO )
CHARACTER         TRANS
INTEGER          INFO, LDA, LDB, N, NRHS
INTEGER          IPIV( * )
DOUBLE PRECISION A( LDA, * ), B( LDB, * )
```



**Informationsbeschaffung zur Numerischen Mathematik im Internet:**

**Diskussionsforen in News–Gruppen:**

<news://news.uni-stuttgart.de/sci.math.num-analysis>

**Software–Bibliotheken im Internet:**

<http://www.netlib.no/>

<http://www.netlib.org/>